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Mid Term Examination Spring 2024

CSE 4745 Numerical Methods

Total Marks: 30 Time: 90 Minutes

[Answer *all* the *three* questions. Figures in the right-hand margin indicate full marks.]

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|---------------|---|------|------|------|------|------|------|------|------------|----|----|----|----|-----|-----|---------------|--|--|--|--|--|--|---|-----|----|
| 1.a) | Draw the <i>block diagram</i> of the process of numerical computing. | 1.5 | CO1 | C1 | | | | | | | | | | | | | | | | | | | | | |
| b) | Write short notes on (any two):
i) Conversion errors ii) Truncation errors iii) Modelling Errors | 2 | CO1 | C2 | | | | | | | | | | | | | | | | | | | | | |
| c) | Describe the <i>banker's rounding rule</i> . Use <i>banker's rounding rule</i> to round off the following numbers to four significant figures -
i) 38.46735 ii) 0.700156 iii) 0.0022213 iv) 19.245101 | 4 | CO2 | C3 | | | | | | | | | | | | | | | | | | | | | |
| d) | What do you mean by <i>absolute error</i> and <i>relative error</i> ? If X = 0.0610958 is rounded off to four significant figures compute the absolute error and relative error in X . | 2.5 | CO2 | C3 | | | | | | | | | | | | | | | | | | | | | |
| 2.a) | What is <i>Horner's rule</i> ? Evaluate the polynomial f(x) = x⁵ - 4x⁴ - 7x³ + 11x - 13 using Horner's rule at x = M . [M means the <i>last digit</i> of your ID number] | 2 | CO2 | C2 | | | | | | | | | | | | | | | | | | | | | |
| b) | Find the root of the equation x³ - x - 1 = 0 , correct to two decimal places, by using the <i>bisection method</i> .
OR
Find the root of the equation 2x³ - 2x - 5 = 0 , correct to two decimal places, by using the <i>secant method</i> .
[<i>secant formula</i> : $x_{n+1} = x_n - ((f(x_n) * (x_n - x_{n-1})) / (f(x_n) - f(x_{n-1})))$] | 5 | CO2 | C3 | | | | | | | | | | | | | | | | | | | | | |
| c) | Derive the <i>Newton - Raphson formula</i> . Write the limitations of Newton - Raphson method. | 3 | CO1 | C2 | | | | | | | | | | | | | | | | | | | | | |
| 3.a) | Find the missing term in the following data using <i>Newton's Binomial Expansion formula</i> .
x 1 2 3 4 5
y 2 5 ? 10 15
Derive the <i>Newton's forward interpolation formula</i> .
OR
Derive the <i>Lagrange's Interpolation formula</i> . | 2 | CO4 | C3 | | | | | | | | | | | | | | | | | | | | | |
| b) | Using a <i>suitable interpolation formula</i> , determine the population of a town in 1895 [if the <i>last digit</i> of your ID is odd] / 1936 [if the <i>last digit</i> of your ID is even], with the help of the following data.
<table border="0"><tr><td>year</td><td>1891</td><td>1901</td><td>1911</td><td>1921</td><td>1931</td><td>1941</td></tr><tr><td>population</td><td>46</td><td>66</td><td>81</td><td>93</td><td>101</td><td>125</td></tr><tr><td>(in millions)</td><td></td><td></td><td></td><td></td><td></td><td></td></tr></table> | year | 1891 | 1901 | 1911 | 1921 | 1931 | 1941 | population | 46 | 66 | 81 | 93 | 101 | 125 | (in millions) | | | | | | | 4 | CO3 | C2 |
| year | 1891 | 1901 | 1911 | 1921 | 1931 | 1941 | | | | | | | | | | | | | | | | | | | |
| population | 46 | 66 | 81 | 93 | 101 | 125 | | | | | | | | | | | | | | | | | | | |
| (in millions) | | | | | | | | | | | | | | | | | | | | | | | | | |
| c) | | 4 | CO4 | C3 | | | | | | | | | | | | | | | | | | | | | |