

**International Islamic University Chittagong**  
 Department of Computer Science and Engineering  
 B. Sc. in CSE, Mid Term Examination, Sprint 2024

Course Code: CSE 2421

Course Title: Computer Algorithms

Time: 1 hour and 30 minutes

Full Marks: 30

[Answer the following questions]

- |  | P | C | D |
|--|---|---|---|
| 1.a) Given an algorithm with a time complexity of $O(n^2)$ and another with a time complexity of $O(n \log n)$ , discuss under what circumstances each algorithm would be preferable in terms of efficiency. Provide real-world examples to support your analysis. | 3 | 2 | 1 |
| b) Discuss the properties of a good algorithm. How do these properties influence the efficiency and effectiveness of an algorithm in solving a given problem?  | 3 | 2 | 1 |
| c) Analyze the time complexity of the following algorithm, which computes the factorial of a non-negative integer $n$ :  | 4 | 2 | 1 |

```
function factorial(n):
    if n equals 0:
        return 1
    else:
        result = 1
        for i from 1 to n:
            result = result * i
        return result
```

Explain the number of operations performed by the algorithm and justify its time complexity using Big O notation. Consider both the best-case and worst-case scenarios.

OR

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| c) Find the complexity of the followings: | 4 | 2 | 1 |
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```
i) void fun(int n) {
    int i, j, k, count = 0;
    for( i= n/2; i<=n; i++)
        for( j=1; j+n/2 <= n; j++)
            for( k=1; k<=n; k=k*2)
                count++;
}
```

```
ii) void fun(int n) {
    if(n <=1) return;
    int i,j;
    for( i=1; i<=n; i++)
        for( j=1; j<=n; j++){
            printf("Hello\n");
            break;
        }
}
```

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| 2. a) Given an array of integers: [7, 2, 1, 6, 8, 5, 3, 4], apply the count-sort algorithm to sort this array. Provide a step-by-step sorting process for the algorithm.                  | 4 | 3 | 1 |
| b) Consider the following recurrence relation:<br>$T(n) = 2T(n/2) + n$<br>Apply the master theorem and recurrence tree method to analyze the time complexity of this recurrence relation. | 3 | 4 | 2 |
| c) Starting with the procedure MAX-HEAPIFY, write pseudocode for the procedure MIN-HEAPIFY(A,i), which performs the corresponding manipulation on a min-heap.                             | 3 | 5 | 2 |

OR

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| c) Show the steps of the operation Extract-min() on the following min-heap<br>$A = \{4, 1, 3, 2, 16, 9, 10, 14, 8, 7\}$                                | 3 | 5 | 2 |
| 3. a) Find an optimal parenthesization of a matrix-chain product whose sequence of dimensions is {6, 5, 4, 8, 6}.                                      | 6 | 3 | 1 |
| b) Given two strings:<br>"abcdefgh" & "acbcfhgh",<br>Apply dynamic programming to find the longest common subsequence (LCS) between these two strings. | 4 | 3 | 2 |

OR

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| b) Explain the concept of dynamic programming in the context of solving optimization problems. Illustrate the dynamic programming approach with an example to find the optimal solution. | 4 | 3 | 2 |
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