

International Islamic University Chittagong  
 Department of Electrical and Electronic Engineering  
 B. Sc. Engineering in EEE  
 Midterm Examination, Spring 2023

Course Code: **MATH-2309**

Course Title: **Mathematics III**

Time: 1 hour 30 minutes

Full Marks: 30

- (i) Answer all the questions. The figures in the right-hand margin indicate full marks.  
 (ii) Course Outcomes (COs) and Bloom's Levels are mentioned in additional Columns.

<b>Course Outcomes (COs) of the Questions</b>	
<b>CO1</b>	This step demonstrates linear algebra's basic idea of vector spaces, subspaces, Linear dependence and independence of vectors, Linear mappings, and Inner product spaces.
<b>CO2</b>	This effort applies the concept of matrix algebra to find the eigenvalues, eigenvectors, and different kinds of matrix decomposition for implementation in the engineering domain.
<b>CO3</b>	Get a basic understanding of scalar and vectors, dot product, cross-product derivative of vectors, and vector integration. Analyse complex engineering problems, know the gradient, divergence, and curl and their physical significance, learn the Greens, Gauss & Stocks theorem and their applications, and be familiar with vector components in spherical and cylindrical systems.

<b>Bloom's Levels of the Questions</b>						
Letter Symbols	R	U	Ap	An	E	C
Meaning	Remember	Understand	Apply	Analyze	Evaluate	Create

- 1) a) Define linearly dependent and independent of vectors. Determine whether or not the vectors in  $\mathbf{R}^3$  are linearly dependent or independent: (i)  $(2, -3, 7), (0, 0, 0), (3, -1, -4)$  and (ii)  $(1, 2, -3), (1, -3, 2), (2, -1, 5)$ . CO1   R,E   5
- 1) b) (i) Define vector subspace. Let  $v \in \mathbf{R}^3$ . Show that  $W$  is not a subspace of  $V$  where  $W = \{a, b, c : a, b, c \in \mathbf{Q}\}$  that is,  $W$  consists of those vectors whose components are rational number. (ii) Define linear combination. For which value of  $K$  will the vector  $A = (1, -2, K)$  in  $\mathbf{R}^3$  be a linear combination of the vectors  $B = (3, 0, -2), C = (2, -1, 5)$ ? CO1   R,Ap   3+2
- 2) a) Consider the following vectors  $v_1 = (1, 2, 1), v_2 = (2, 9, 0), v_3 = (3, 3, 4)$  then the set  $S = \{v_1, v_2, v_3\} \subset V$ , where  $V = \mathbf{R}^3$  is a vector space, then prove that  $S$  is a basis of  $V$  and find its dimension. CO1   E   6

- 2) b) If  $V = \{(x, y, z) : x, y, z \in \mathcal{R}\} = \mathcal{R}^3$  and  $W = \{(x, y, 0) : x, y \in \mathcal{R}\}$  are two vector spaces over the field  $F$ . then prove that the transformation/mapping  $L: V \rightarrow W$  is defined by  $L(x, y, z) = (x, y, 0)$  is linear transformation (Linear Mapping). .CO1 An 4
- 3) a) Using the Gram Schmidt orthogonalization process to construct the basis  $\{u_1, u_2, u_3\}$  into an orthogonal basis where  $u_1 = (1, 1, 1)$ ,  $u_2 = (0, 1, 1)$  and  $u_3 = (0, 0, 1)$  CO1 Ap 6
- 3) b) Verify that the following is an inner product in  $\mathcal{R}^2$ ,  $\langle u, v \rangle = x_1y_1 - x_1y_2 - x_2y_1 + 3x_2y_2$ , where  $u = (x_1, x_2)$ ,  $v = (y_1, y_2)$  CO1 Ap 4

OR

- 3) a) Apply the Gram Schmidt orthogonalization process for QR decomposition for the matrix  $A = \begin{pmatrix} 1 & 3 \\ -1 & 4 \end{pmatrix}$ . CO1 Ap 6
- 3) b) Define the inner product space then, if  $f(t) = 3t - 5$ ,  $g(t) = t^2$  then find the inner product of  $\langle f, g \rangle$ . CO1 Ap 4